

# SEM 2: Structural Equation Modeling

Week 2 - Causal modeling

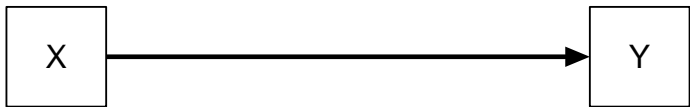
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## Causal modeling

- ▶ This course will introduce structural equation modeling (SEM)
- ▶ In SEM, we will discuss modeling complex causal hypotheses
- ▶ Again, all variables are assumed normally distributed and all associations are assumed linear
- ▶ Causal hypotheses can be specified between observed and latent variables
- ▶ CFA is a special case of SEM

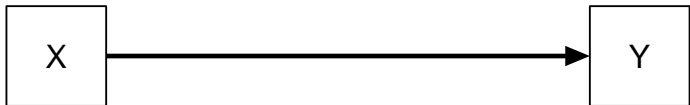
## Causal models



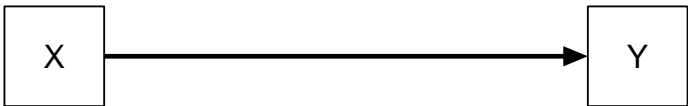
$X$  causes  $Y$

## Endogenous and exogenous

- ▶ **Exogenous** (independent) variables are variables of which the causal origin are not modeled
  - ▶ Exogenous variables have a variance (sometimes not drawn)
  - ▶ Exogenous variables, except residuals, are allowed to covary (sometimes not drawn)
  - ▶ Latents:  $\xi$  ( $\xi_i$ ); observed:  $x$  ( $x$  is also used for indicators of latent exogenous variables)
  - ▶ Residuals are exogenous
- ▶ **Endogenous** (dependent) variables are variables of which the causal origin are modeled
  - ▶ Simply stated: endogenous variables have incoming arrows
  - ▶ Endogenous variables do **not** have a variance by themselves
  - ▶ Latents:  $\eta$  ( $\eta$ ); observed:  $y$
  - ▶ The causal equation for endogenous variables can be derived from the path diagram by summing all incoming edges

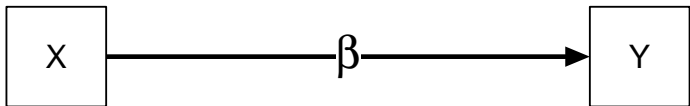


$X$  is exogenous,  $Y$  is endogenous

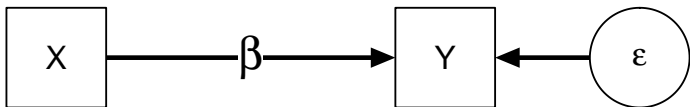


$$y_i = x_i$$

Causal effect goes from right hand side to left hand side.  
Experimentally changing  $x$  will change  $y$ , experimentally changing  $y$  will **not** change  $x$



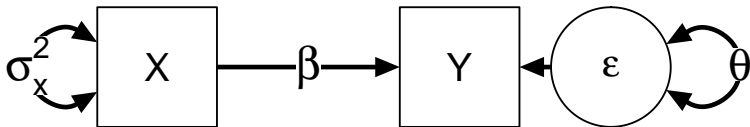
$$y_i = \beta x_i$$



$$y_i = \beta x_i + \varepsilon_i$$



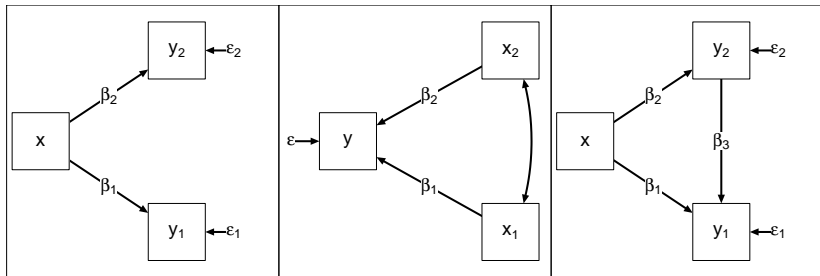
Exogenous variables have a variance (often not drawn)



$$y_i = \beta x_i + \varepsilon_i$$

$$x \sim N(\mu_x, \sigma_x)$$

$$\varepsilon \sim N(0, \theta)$$



Goal: derive a model to explain (co)variances related to observed **endogenous** variables (including covariances between observed endogenous and exogenous variables), using parameters and (co)variances of observed and unobserved **exogenous** variables.