

# Network Psychometrics



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# **Network Psychometrics**

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Faculteit: Faculteit der Maatschappij- en Gedragswetenschappen

*In loving memory of*



*Janneke de Kort*

26/01/1984 - 25/05/2016



*Zara Bamdad*

19/03/1990 - 15/07/2016



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